Describing Data Student Guide

Math 6 Unit 8 Accelerated Part 2

desmos Unit 7.8, Student Goals and Glossary

Glossary

Term	Definition		
experiment	An experiment is something you can do over and over again, and you don't know what will happen each time. For example, each time you spin the spinner, it could land on red, blue, or green.	Red Blue Green	
event	An event is a set of one or more outcomes in a chance experiment. For example, if we roll a number cube, there are six possible outcomes.		
mean	The mean is one way to measure the center of a data set. We can think of it as a balance point. For example, for the data set 7, 9, 12, 13, 14, the mean is 11.	4 2 4 2 2 4 2 4 2 4 2 4 2 4 2 4 2 4 2 4 2 4 2 4 2 4 4 2 4 2 4 4 2 4 4 2 4 4 2 4 4 1 1 1 1 1 1 1 1	
mean absolute deviation (MAD)	The mean absolute deviation is one way to measure how spread out a data set is. Sometimes we call this the MAD. To find the MAD, add up the distance between each data point and the mean. Then, divide by how many numbers there are. For example, in this data set, the MAD is $\frac{4+2+1+2+3}{5} = \frac{12}{5}$ because there are 5 data points and each is a different distance away from the mean. These travel times are typically $\frac{12}{5}$ or 2.4 minutes away from the mean.	$4 \xrightarrow{3} \xrightarrow{4} \xrightarrow{2} \xrightarrow{2} \xrightarrow{4} \xrightarrow{7} 8 \xrightarrow{9} 10 \xrightarrow{11} 12 \xrightarrow{13} 14$ Travel Time in Minutes	

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median	The median is one way to measure the center of a data set. It is the middle number when the data set is listed in order.For data set A, the median is 12.Set A: 7, 9, 12, 13, 14Set B: 2, 5, 11, 12		
	For data set B, there are two numbers in the middle. Set B: 3, 5, 11, 12 The median is the average of those numbers: $\frac{5+11}{2} = 8.$		
interquartile range (IQR)	The interquartile range is one way to measure how spread out a data set is. We also call this the IQR. To find the interquartile range, we subtract the first quartile from the third quartile. For example, the IQR of this data set is 20 because $50 - 30 = 20$.		
	22 29 30 31 31 43 44 45 50 50 59 Q1 Q2 Q3 Q3 Q3 Q3 Q3 Q3		
outcome	An outcome of a chance experiment is one of the things that can happen when you do the experiment. For example, the possible outcomes of tossing a coin are heads and tails.		
population	A population is a set of people or things that we want to study. For example, if we want to study the heights of people on different sports teams, the population would be all the people on the teams.		
probability	The probability of an event is a number that tells how likely it is to happen. A probability of 1 means the event will always happen. A probability of 0 means the event will never happen. For example, the probability of spinning red is $\frac{1}{4}$.		
random	Outcomes of a chance experiment are random if they are all equally likely to happen.		

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representative	A sample is representative of a population if its distribution resembles the population's distribution in center, shape, and spread.	
sample	A sample is part of a population. For example, a population could be all the seventh grade students at one school. One sample of that population is all the seventh grade students who are in band.	
sample space	The sample space is the list of every possible outcome for a chance experiment. For example, the sample space for tossing two coins is: heads-heads, tails-heads, heads-tails, tails-tails.	
simulation	A simulation is an experiment that is used to estimate the probability of a real-world event. For example, suppose the weather forecast says there is a 25% chance of rain. We can simulate this situation with a spinner. If the spinner stops on red, it represents rain. If not, it represents no rain.	

desmos Unit 7.8, Family Resource

Unit 8 Summary

Prior Learning	Math 7, Unit 8	Future Learning
Math 6Statistical variabilityData distributions	ProbabilitySampling	Math 8, Unit 6 Scatter plots Lines of best fit
 Math 7 Proportional reasoning (Unit 2) Percent change (Unit 4) 	 Using center and variability to compare populations. 	

Probability

A *probability* is a number that represents how likely something is to happen.

If you flip a coin, the probability of the coin landing heads up is 0.5.

The probability that the coin turns into a bunny is 0.

When you repeat an experiment, the results get closer and closer to the probability.

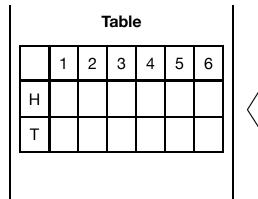
If you flip a coin 100 times, it might land heads up 50 times, 49 times, 52 times, or maybe even 60 times. As you flip the coin more times, the fraction of heads gets closer to 0.5.

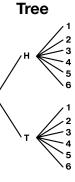
0.9 0.8 0.7 0.6 0.5 0.4 0.3 0.2 0.1 0 100 200 300 400 Number of Flips

In an experiment, it is often helpful to know the sample space, a list of every possible outcome.

Here are two ways to represent the 12 possible outcomes of flipping a coin and then rolling a number cube.









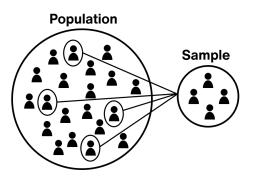
Fraction of Flips That Are Heads

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Sampling

Sometimes we want to know information about a group, but the group is too large for us to be able to ask everyone. It can be useful to collect data from a *sample* (some of the group) of the *population* (the whole group).

For example, we might want to know what percentage of Americans work from home. It would be too challenging to ask all Americans, so we can ask a smaller sample of working Americans.





If our sample is some employees at a grocery store, we may get very different results than if our sample is some employees of a technology company. Neither sample is representative of the population of all working Americans.

A sample selected at random is most likely to be *representative* of the population because it has the chance to include all kinds of working adults.

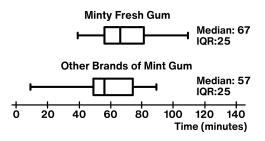
We can use samples to estimate information about a population and to make comparisons.

For example, the Minty Fresh company collects data from a sample of gum buyers to see how many minutes it takes for their mint gum to lose flavor compared to other brands.

These box plots show that the median time for the sample of Minty Fresh Gum is longer than the sample of other brands.

However, there may not be a difference between two populations because there is a lot of overlap between the two samples, and because the difference in the medians is less than one IQR (interquartile range).

If you are interested in learning more about how these statistical measures are calculated, see the <u>Statistics Summary</u>.



Try This at Home

Probability

DesPops makes a mystery lollipop. Each lollipop is one of these flavors: strawberry, lime, pineapple, or mango, but you don't know which flavor you have until you try it.

- 1.1 What is the probability of getting a strawberry flavored lollipop?
- 1.2 Would it be surprising to buy 5 lollipops and none were strawberry? Explain your thinking.
- 1.3 Hailey says that if she buys 200 lollipops, exactly 50 of them will be mango. Explain to Hailey what is incorrect about her reasoning.

A game uses cards that say "forward" or "backward" and a spinner numbered from 1 to 5. On their turn, a player picks a card and spins the spinner to find out which way and how much to move.

- 2.1 How many different outcomes are possible?
- 2.2 What is the probability that the next player will get to move their piece forward 5 spaces?
- 2.3 What is the probability that the next player will have to move their piece backward an odd number of spaces?

Sampling

A city council wants to know how many buildings in the city have lead paint, but they don't have enough time to test all 100 000 buildings in the city. They want to test a sample of buildings that will be representative of the population.

- 3.1 Describe a way to pick a sample that **is likely** to be representative of the population.
- 3.2 Describe a way to pick a sample that **is not likely** to be representative of the population.

Each year Brielle measures a random sample of her tomato plants.

Here is her data for the past two years.

4. Brielle is nervous that her garden this year isn't as healthy as last year's. Do you agree? Use at least one piece of evidence to support your claim.

Tomato Plant Heights

Last Year Mean: 55 inches MAD: 7.8 inches

This Year Mean: 50.5 inches MAD: 8 inches

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Solutions:

1.1
$$\frac{1}{4}$$
 (or equivalent)

- 1.2 No. *Explanations vary.* With a sample of only 5 lollipops, it isn't surprising. The more lollipops you buy, the closer the fraction of strawberry lollipops will get to the probability.
- 1.3 *Responses vary.* Even though about 25% of your lollipops will be mango, we do not know exactly how many will be. It might be 50 lollipops, slightly more, or slightly less. There is even a small chance it will be way more or less than 50.
- 2.1 10 possible outcomes

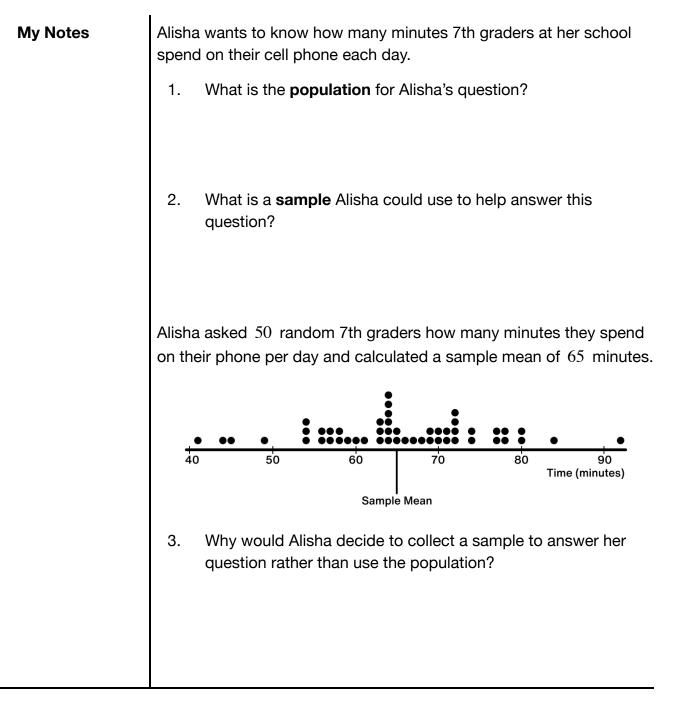
2.2
$$\frac{1}{10}$$
 (or equivalent)

- 2.3 $\frac{3}{10}$ (or equivalent)
- 3.1 Responses vary.
 - Put the addresses of all the buildings into a computer and have the computer select 50 addresses randomly from the list.
 - Put all of the street names in a bag. Pick several streets randomly and then test all the houses on that street.
- 3.2 Responses vary.
 - Testing all the same type of buildings (like all the schools or all the gas stations).
 - Testing buildings all in the same location, such as the buildings closest to city hall.
 - Testing all the newest buildings or all of the oldest buildings.
 - Testing a small number of buildings, like 5 or 10.
- 4. No, she does not need to be nervous.

Explanations vary. Even though this year, the mean height of her sample is less than it was last year, the difference is not that big. This year's plants are 4.5 inches shorter than last year's, which is less than the MAD. This means it's more likely that she just happened to end up with smaller plants in her sample, but that the populations are not that different.

Unit 7.8, Lesson 10: Notes

Name _



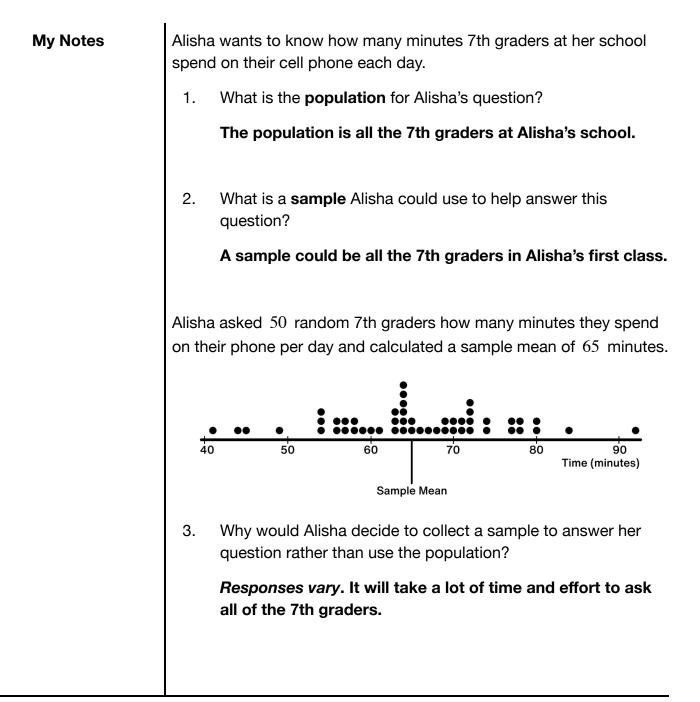
Summary

 \Box I can explain what a sample is and when it is useful.

I can compare the means of samples to the mean of the population.

Unit 7.8, Lesson 10: Notes

Name _



Summary

 \Box I can explain what a sample is and when it is useful.

I can compare the means of samples to the mean of the population.

Unit 7.8, Lesson 11: Notes

Name _____

My Notes	1. In your own words, explain what it means for a sample to be <i>representative</i> of a population.		
	2. Match each headline with method that most likely pro		
	Headline	Sampling Method	
	One Quarter of Working Americans Spend Time Working From Home!	A. Ask all 100 employees at one technology company.	
	Most Americans Spend Time Working From Home!	B. Ask all the employees at 100 random grocery stores.	
	Almost No One Works From Home!	C. Call random phone numbers until you ask 100 people.	
	3. Which sampling method ab representative sample? Exp	ove is most likely to produce a plain your thinking.	

Summary

 \Box I can explain why a sampling method is or is not likely to produce a biased sample.

Unit 7.8, Lesson 11: Notes

Name _____

My Notes	 <i>representative</i> of a population There is data in your sepopulation. For example, grade or class. A sample is represent version of the population dogs and half cats in the population dogs and half cats in the section of the section with the section of the section	 representative of a population. Responses vary. There is data in your sample from many parts of the population. For example, it is not only people from one grade or class. A sample is representative if it looks like a smaller version of the population. If there are half dogs and half cats in the population, then there should be about half dogs and half cats in the sample. 	
	Headline	Sampling Method	
	_C. One Quarter of Working Americans Spend Time Working From Home!	A. Ask all 100 employees at one technology company.	
	A. Most Americans Spend Time Working From Home!	B. Ask all the employees at 100 random grocery stores.	
	_ B. _Almost No One Works From Home!	C. Call random phone numbers until you ask 100 people.	
	 Which sampling method ab representative sample? Exp 	ove is most likely to produce a blain your thinking.	
	-	nd B could both be biased because by company or at grocery stores I working Americans.	

Summary

 \Box I can explain why a sampling method is or is not likely to produce a biased sample.

desmos 🗐 Unit 7.8, Lesson 12: Notes

Name _____

My Notes

Cameron bought a bag of White Flower Seed Mix and is curious how many flowers of each type there are. Cameron planted 25 seeds, and these were the results.

Flower Type	Count	Percentage
Daisy	14	
White Zinnia	5	
Aster	6	
Total	25	



- 1. Complete the table with the percentage of each flower type.
- 2.1 Estimate how many of the 600 seeds in the bag will be asters. Organize your calculations so others can follow them.

2.2 What could you do to be more confident in your estimate?

Summary

 \Box I can use proportional reasoning and a sample to estimate information about a population.

desmos 🗐 Unit 7.8, Lesson 12: Notes

Name ___

My Notes

Cameron bought a bag of White Flower Seed Mix and is curious how many flowers of each type there are. Cameron planted 25 seeds, and these were the results.

Flower Type	Count	Percentage
Daisy	14	56%
White Zinnia	5	20%
Aster	6	24%
Total	25	100%



- 1. Complete the table with the percentage of each flower type.
- 2.1 Estimate how many of the 600 seeds in the bag will be asters. Organize your calculations so others can follow them. *Calculations vary.*
 - 24% of $600 = 0.24 \cdot 600 = 144$ asters
 - $25 \cdot 24 = 600$ and $6 \cdot 24 = 144$ asters
- 2.2 What could you do to be more confident in your estimate? *Responses vary.*
 - You could plant more samples of 25 seeds and see if the results are similar between the samples.
 - You could plant a larger sample, like 100 seeds. A larger sample might be more accurate.

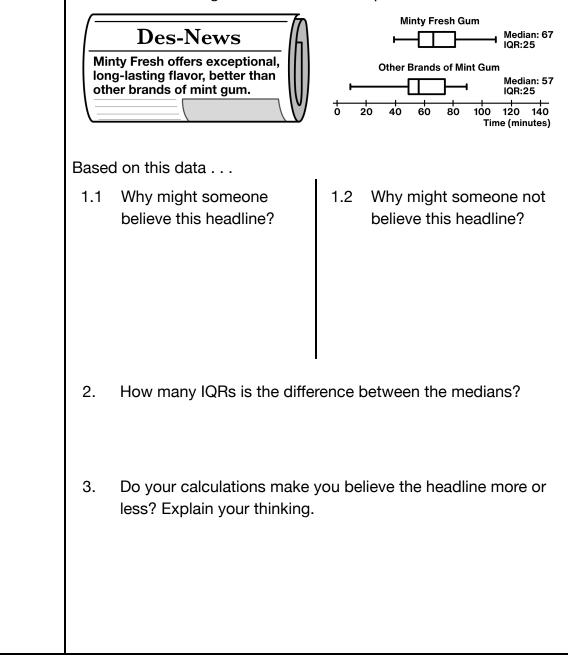
Summary

desmos 🗐 Unit 7.8, Lesson 14: Notes

Name _

My Notes

The Minty Fresh company collects data to see how many minutes it takes for their mint gum to lose flavor compared to other brands.



Summary

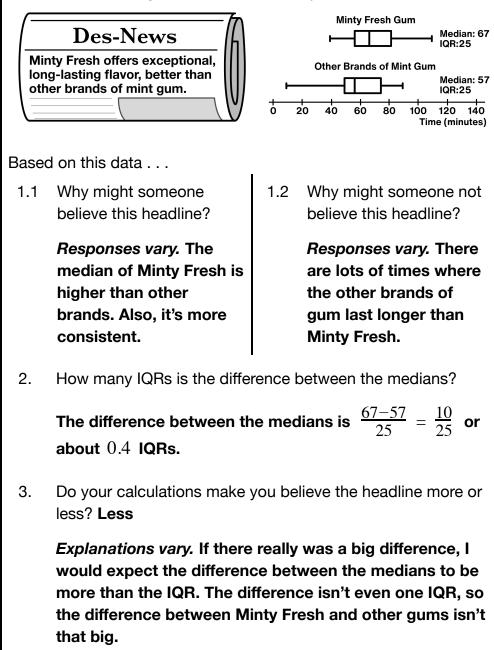
I can use measures of center and the variability of two samples to decide if two populations are very different.
 I can use a measure of variability to explain the difference between measures of center.

desmos 自 Unit 7.8, Lesson 14: Notes

Name _

My Notes

The Minty Fresh company collects data to see how many minutes it takes for their mint gum to lose flavor compared to other brands.



Summary

I can use measures of center and the variability of two samples to decide if two populations are very different.

I can use a measure of variability to explain the difference between measures of center.

Unit 7.8, Lesson 15: Notes

Name __

My Not	tes
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Here is a sample of asthma rates from Montgomery, Alabama.

Number of Adults Who Have Asthma (per 1 000)
112
105
93
129
127
125
93

One of the asthma rates is 116.

- 1.1 What does this number mean?
- 1.2 Why might someone be interested in this data?
- 2. Based on this data, what is the average asthma rate in Montgomery?

Here are statistics based on a sample from Atlanta, Georgia.

- 3. How does the asthma rate in Montgomery compare to the asthma rate in Atlanta? Mean: ≈ 115
 - Median: 116 IQR: 10

MAD: ≈ 9.2

Summary

I can compare two groups by taking random samples, then calculating and interpreting the statistics.

Note: The data is derived from Centers for Disease Control and Prevention, National Center for Chronic Disease and Health Promotion, Division of Population Health, Atlanta, GA based on BRFSS 2018 or 2017, Census 2010 population counts or census county population estimates of 2018 or 2017, and ACS 2014-2018 or ACS 2013-2017.

desmos Unit 7.8, Lesson 15: Asthma Rates

Name ____

My Notes

Here is a sample of asthma rates from Montgomery, Alabama.

Number of Adults Who Have Asthma (per 1 000)
112
105
93
129
127
125
93

One of the asthma rates is 116.

1.1 What does this number mean?

Responses vary. This number means that 116 adults out of every $1\,000$ adults in that community have asthma.

- 1.2 Why might someone be interested in this data? *Responses vary.*
 - They might want to know how much asthma medication is needed in the city.
 - They could be curious how this might affect them and their children.
- 2. Based on this data, what is the average asthma rate in Montgomery?

Mean: 112 adults per 1000

Median: 112 adults per 1000

Mean: ≈ 115

MAD: ≈ 9.2

Median: 116

IQR: 10

Here are statistics based on a sample from Atlanta, Georgia.

3. How does the asthma rate in Montgomery compare to the asthma rate in Atlanta? Asthma Rates

Responses vary. The average asthma rate in Atlanta is higher than the average in Montgomery, but there isn't a big difference. The difference is about

3 adults, which is less than one MAD.

Summary

☐ I can compare two groups by taking random samples, then calculating and interpreting the statistics.

Unit 7.8, Lesson 2: Notes

Name _____

My Notes		letters PROBABILITY are in a bag. In an experiment, one letter is ted at a time and returned to the bag. What is the sample space for this experiment?		
	1.			
	2.	Describe how to d the bag on the nex	etermine the probability of picking a Y from t pick.	
	Write	the probability of ea	ach event happening on the next pick.	
	3.	Picking the letter B from the bag.		
	4.			
	5.			
	6.	Picking the letter S from the bag.		
	7.		 Label the pieces in the bag so that it has these probabilities on the next pick: The probability of picking a P is 1/4. The probability of picking a B is 0. The probability of picking a G is equal to the probability of picking an R. 	

Summary

□ I can determine the probability of an event using its sample space.

 \Box I can compare probabilities written as fractions, decimals, and percentages.

Unit 7.8, Lesson 2: Notes

Name _____

My Notes	he letters PROBABILITY are in a bag. In an experiment, one letter is icked at a time and returned to the bag.			
	1. What is the sample space for this experiment?			
	The sample space is the letters P, R, O, B, A, B, I, L, I, T, Y	<i>ſ</i> .		
	2. Describe how to determine the probability of picking a Y from the bag on the next pick.	n		
	Responses vary. Count the letters in the sample space (11)		
	and see how many are a Y (1). The probability is $\ rac{1}{11}$.			
	Write the probability of each event happening on the next pick.			
	3. Picking the letter P from the bag. $\frac{1}{11}$			
	4. Picking the letter B from the bag. $\frac{2}{11}$			
	5. Picking the letters B or I from the bag. $\frac{4}{11}$			
	6. Picking the letter S from the bag. 0			
	7. Label the pieces in the bag so that it has these probabilities on the next pick:	>		
	• The probability of picking a P is $\frac{1}{4}$.			
	• The probability of picking a B is 0.			
	• The probability of picking a G is equal to the probability of picking an R.			

Summary

□ I can determine the probability of an event using its sample space.

 \Box I can compare probabilities written as fractions, decimals, and percentages.

desmos 🗐 Unit 7.8, Lesson 3: Notes

Name _____

My Notes There are 6 blocks in a bag. The table shows results from			
	Block Number Color of Picks		 Based on these results, how many of the 6 blocks are red?
	Purple 32		
	Red	68	Explain your thinking.
picki 2.2 Abou do y		ing a green ut how man	here the probability of block is 60%. The times out of 50 picks or pick a green block?

Summary

□ I know that sometimes outcomes of an experiment are not equally likely.

□ I can use proportional reasoning with data from a repeated experiment to make predictions.

desmos 🗐 Unit 7.8, Lesson 3: Notes

I

Name _____

My Notes	Ther	e are 6	blocks in a	bag. Th	e table shows results	s from 100 picks
		lock Solor	Number of Picks	1.	Based on these rest of the 6 blocks are	•
	Р	urple	32		4 bloc	cks
		Red	68		Explain your thinkii	ng.
					Explanations vary	$\frac{68}{100}$ is 68%,
					and 68% of 6 blo blocks.	ocks is about 4
	2.1	pick	ign a bag wl ing a green s vary.		probability of 60%.	
			•		d 2 red blocks d 4 blue blocks	
	2.2				out of 50 picks green block?	
		Abo	ut 30 times	5.		
		the	blocks are g	green, l	Explanations vary. would expect to pi the time. 60% of 5	ick a green

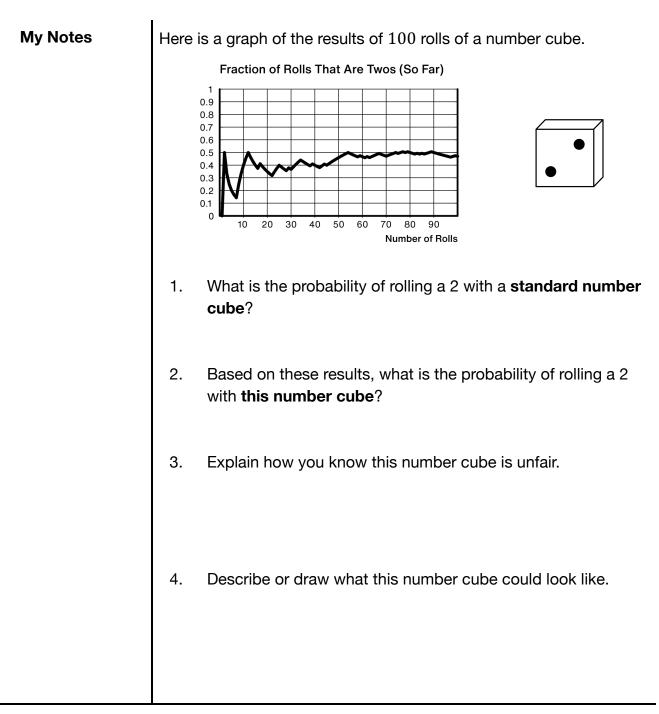
Summary

□ I know that sometimes outcomes of an experiment are not equally likely.

I can use proportional reasoning with data from a repeated experiment to make predictions.

desmos 🗐 Unit 7.8, Lesson 5: Notes

Name



Summary

I can decide whether or not something is fair based on the results of a repeated experiment.

I can use the results from a repeated experiment to approximate the probability of an event.

desmos 🗐 Unit 7.8, Lesson 5: Notes

Name _____

My Notes	Here is a graph of the results of 100 rolls of a number cube.
	Fraction of Rolls That Are Twos (So Far)
	0.1 0 10 20 30 40 50 60 70 80 90 Number of Rolls
	1. What is the probability of rolling a 2 with a standard number cube ?
	$\frac{1}{6}$
	2. Based on these results, what is the probability of rolling a 2 with this number cube ?
	0.5 or $\frac{1}{2}$
	3. Explain how you know this number cube is unfair.
	Explanations vary. If the number cube were fair, the graph
	would be getting closer to $\frac{1}{6}$. This graph got closer to $\frac{1}{2}$
	which means that rolling a 2 is more likely than it should be.
	4. Describe or draw what this number cube could look like.
	Responses vary.
	 Half of the sides are 2s. The other half are 3s. The cube has the numbers 1, 2, 2, 2, 5, and 6 on it.

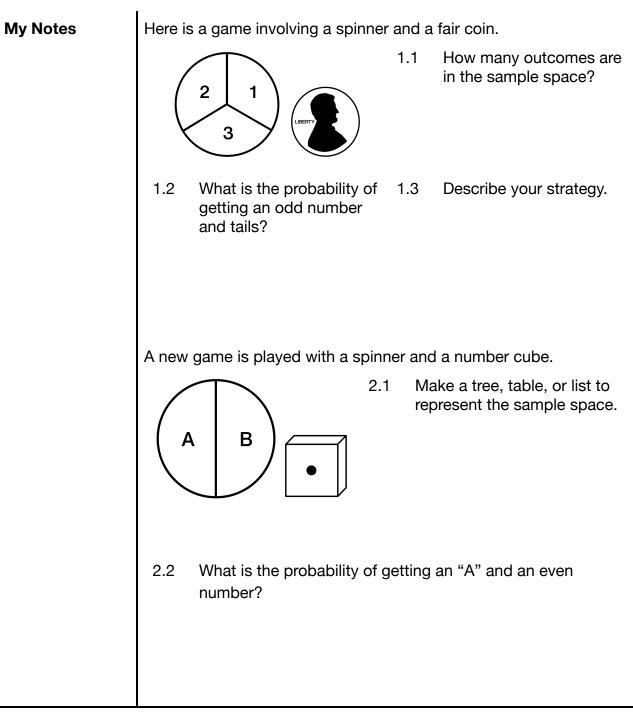
Summary

□ I can decide whether or not something is fair based on the results of a repeated experiment.

□ I can use the results from a repeated experiment to approximate the probability of an event.

Unit 7.8, Lesson 6: Notes

Name ____

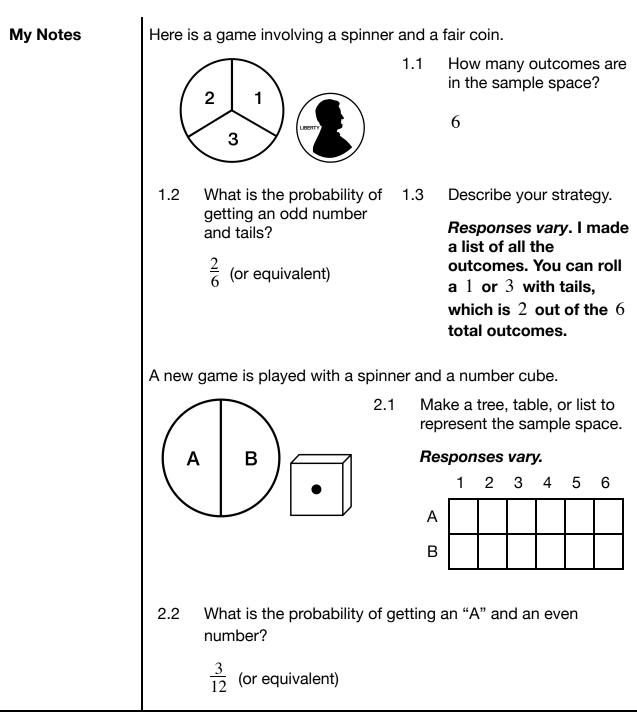


Summary

I can write out the sample space for a multistep experiment using a list, table, or tree diagram.
 I can calculate the probability of a multistep event.

Unit 7.8, Lesson 6: Notes

Name __



Summary

□ I can write out the sample space for a multistep experiment using a list, table, or tree diagram.

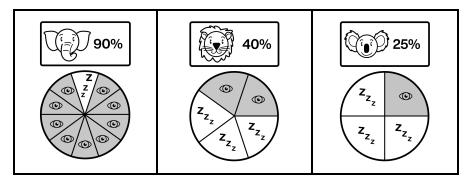
I can calculate the probability of a multistep event.

desmos 🗐 Unit 7.8, Lesson 7: Notes

Name _____

My Notes

Brianna designed a simulation to help her estimate the probability of seeing her three favorite animals awake when she visits the zoo.



1. Describe how Brianna could use these spinners to estimate the probability that at least two of her favorite animals will be awake when she visits the zoo.

The table shows the results of 300 experiments with the spinners.

Experiments with	Count	Percentage
No animals awake	12	4%
1 animal awake	171	57%
2 animals awake	105	35%
3 animals awake	12	4%

2. Estimate the probability that at least 2 of Brianna's favorite animals will be awake when she visits the zoo.

Summary

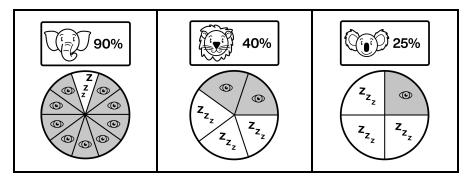
I can use a simulation to estimate the probability of a multistep real-world event.
I can connect real-world situations and the probability tools I could use to simulate those situations.

desmos 🗐 Unit 7.8, Lesson 7: Notes

Name _____

My Notes

Brianna designed a simulation to help her estimate the probability of seeing her three favorite animals awake when she visits the zoo.



1. Describe how Brianna could use these spinners to estimate the probability that at least two of her favorite animals will be awake when she visits the zoo.

Responses vary. Briana could run a lot of experiments and record how many of the experiments had at least two spinners land on an open eye.

The table shows the results of 300 experiments with the spinners.

Experiments with	Count	Percentage
No animals awake	12	4%
1 animal awake	171	57%
2 animals awake	105	35%
3 animals awake	12	4%

2. Estimate the probability that at least 2 of Brianna's favorite animals will be awake when she visits the zoo.

39%

Summary

I can use a simulation to estimate the probability of a multistep real-world event.
I can connect real-world situations and the probability tools I could use to simulate those situations.